

Probability

- Mutually exclusive** – two events are mutually exclusive if they cannot happen at the same time
- Exhaustive** – events are exhaustive if they include all outcomes
- Experimental probability** – the frequency of an event/total frequency
- Independent** – two events are independent if the results of one does not affect the other
- Sample space diagram** – this shows all the possible outcomes of two events
- Venn diagram** – a set of overlapping circles that can be used to show probabilities
- Tree diagram** – this shows two or more events and their probabilities

Statistics – Probability

Introduction

The likelihood of an event happening

	1/4	1/2	3/4	
0%	25%	50%	75%	100%
0	0.25	0.5	0.75	1

Impossible
Even Chance
Certain

Calculating probability

$P(\text{Event}) = \frac{\text{number of successful outcomes}}{\text{total number of outcomes}}$

$P(3) = \frac{2}{8} \Rightarrow \frac{1}{4}$

Simplify answers where possible

Types of events

Mutually exclusive
 Events that cannot happen at the same time
 Rolling a die $\rightarrow P(1 \text{ and } 6)$

All probabilities from the event will sum to make 1

Independent events
 Events where the outcome of one doesn't affect the outcomes of the others
 Picking a counter out of a bag, replacing it and repeating.

The 'OR' rule (mutually exclusive)

$P(a \text{ or } b) = P(a) + P(b)$

$P(2 \text{ or } 4) = \frac{2}{8} + \frac{1}{8} \Rightarrow \frac{3}{8}$

Add each probability

The 'AND' rule (independent)

$P(a \text{ and } b) = P(a) \times P(b)$

$P(2 \text{ tails}) = \frac{1}{2} \times \frac{1}{2} \Rightarrow \frac{1}{4}$

Multiply each probability

Counting outcomes

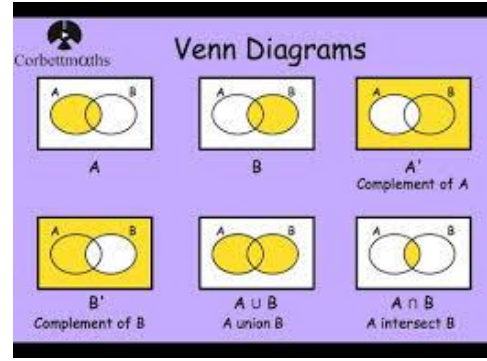
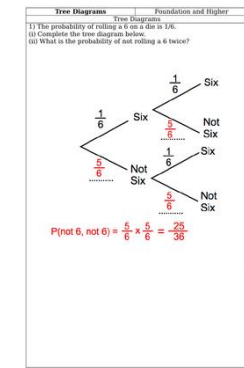
Working out how many combinations there are

Rolling a die and flipping a coin

	1	2	3	4	5	6
Heads	H, 1	H, 2	H, 3	H, 4	H, 5	H, 6
Tails	T, 1	T, 2	T, 3	T, 4	T, 5	T, 6

This is a sample space diagram

There are **12** possible outcomes from this event



Higher GCSE only – set notation and conditional probability

Monday, 12 October 2015

Dependent Events - Probability Trees

In a bag there are 7 blue and 5 red sweets. Draw a Tree Diagram to show all possible outcomes when 2 sweets are drawn out and not replaced.

P(B, B)	$\frac{7}{12} \times \frac{6}{11} = \frac{42}{132} = \frac{7}{22}$
P(B, R)	$\frac{7}{12} \times \frac{5}{11} = \frac{35}{132}$
P(R, B)	$\frac{5}{12} \times \frac{6}{11} = \frac{30}{132}$
P(R, R)	$\frac{5}{12} \times \frac{4}{11} = \frac{20}{132}$