

Angles and trigonometry

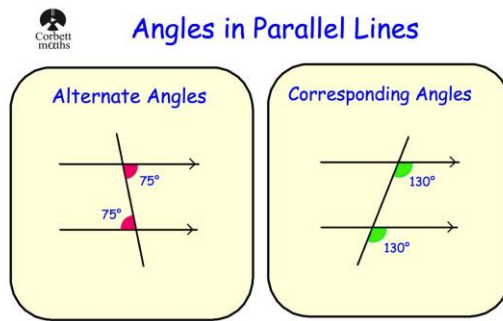
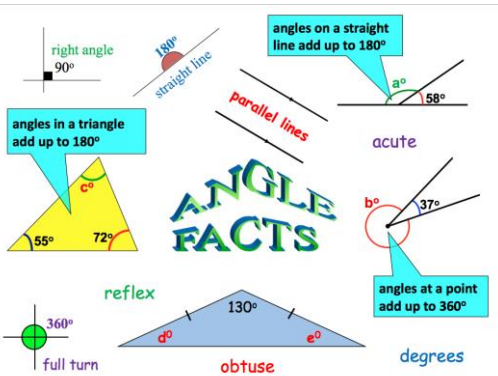
Congruent – shapes are exactly the same size and shape

Similar – one shape is an enlargement of the other

Regular polygon – a shape with equal sides and equal angles

Tessellate – when shapes fit together with no gaps, the angles where the shapes meet must add up to 360°

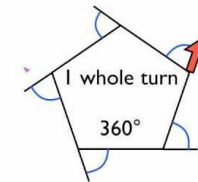
Hypotenuse – the longest side in a right angled triangle



Angles in regular polygons

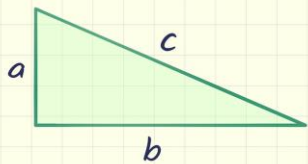
Shape	Sides	Interior Angles	Shape	Each Angle
Triangle	3	180°		60°
Quadrilateral	4	360°		90°
Pentagon	5	540°		108°
Hexagon	6	720°		120°
Heptagon (or Septagon)	7	900°		128.57...°
Octagon	8	1080°		135°
Nonagon	9	1260°		140°
...
Any Polygon	n	(n-2) × 180°	n	(n-2) × 180° / n

Exterior angles



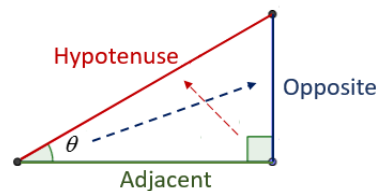
Higher GCSE only, advanced trigonometry and trigonometric graphs

Pythagoras Theorem



$$a^2 + b^2 = c^2$$

SOHCAHTOA

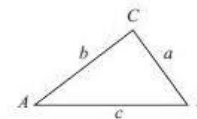


SOH $\sin \theta = \frac{\text{Opposite}}{\text{Hypotenuse}}$

CAH $\cos \theta = \frac{\text{Adjacent}}{\text{Hypotenuse}}$

TOA $\tan \theta = \frac{\text{Opposite}}{\text{Adjacent}}$

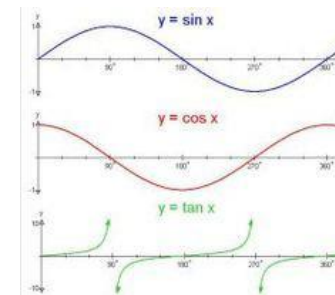
In any triangle ABC



Sine Rule $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

Cosine Rule $a^2 = b^2 + c^2 - 2bc \cos A$

Area of triangle $= \frac{1}{2}ab \sin C$



Transformation Rules for Functions

Function Notation	Type of Transformation	Change to Coordinate Point
$f(x) + d$	Vertical translation up d units	$(x, y) \rightarrow (x, y + d)$
$f(x) - d$	Vertical translation down d units	$(x, y) \rightarrow (x, y - d)$
$f(x + c)$	Horizontal translation left c units	$(x, y) \rightarrow (x - c, y)$
$f(x - c)$	Horizontal translation right c units	$(x, y) \rightarrow (x + c, y)$
$-f(x)$	Reflection over x-axis	$(x, y) \rightarrow (x, -y)$
$f(-x)$	Reflection over y-axis	$(x, y) \rightarrow (-x, y)$
$af(x)$	Vertical stretch for $ a > 1$	$(x, y) \rightarrow (x, ay)$
	Vertical compression for $0 < a < 1$	
$f(bx)$	Horizontal compression for $ b > 1$	$(x, y) \rightarrow \left(\frac{x}{b}, y\right)$
	Horizontal stretch for $0 < b < 1$	